

Assignment #3

1. Give an example of a statement $P(x,y)$ such that

$$\sim((\forall x, \exists y, P(x,y)) \Rightarrow (\exists y, \forall x, P(x,y)))$$

Use Natural Deduction to prove the following
(where $P(x), P(x,y), Q(x), R(x)$ are statements)

2. $\forall x, P(x)$ or $\sim P(x)$
3. $x = y$ and $y = z \Rightarrow x = z$
4. $(\sim \exists x, P(x)) \Rightarrow \forall x, \sim P(x)$
5. $\sim(\forall x, \exists y, P(x,y)) \Rightarrow \sim(\exists y \forall x (P(x,y)))$
6. $(\forall x, R(x) \Rightarrow (Q(x) \Rightarrow P(x))) \Rightarrow ((\exists x, R(x) \text{ and } Q(x)) \Rightarrow (\exists x, R(x) \text{ and } P(x)))$
7. $(\exists! x, P(x) \text{ or } Q(x))$ and $(\forall x, \sim P(x)) \Rightarrow (\exists! x, Q(x))$